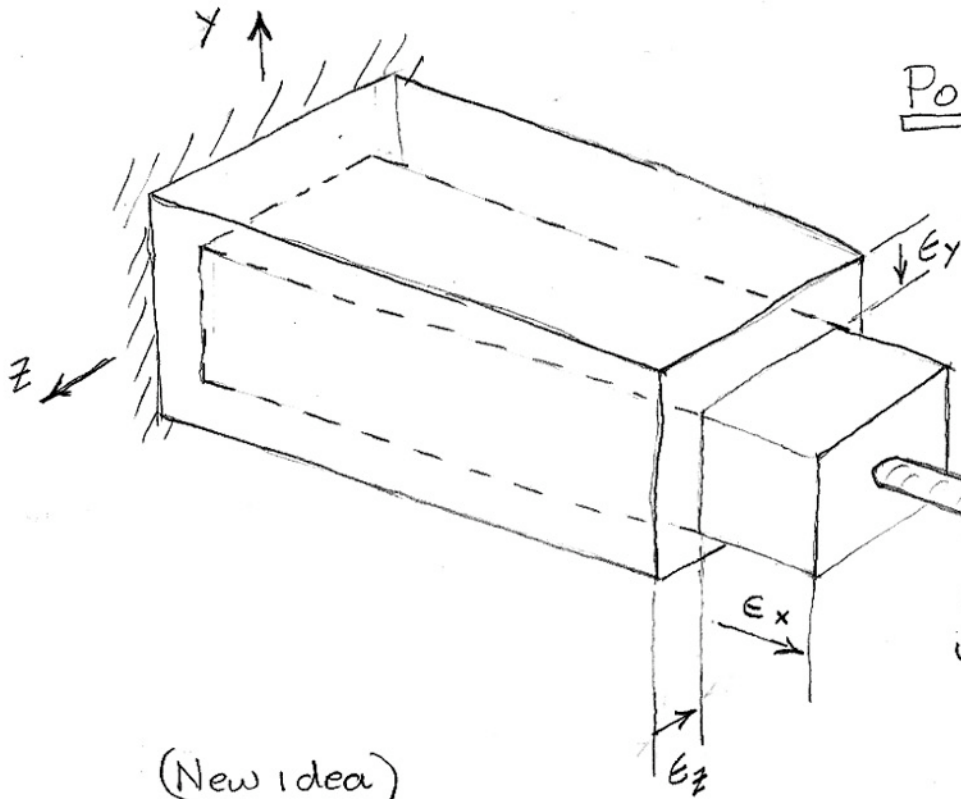


Poisson's Ratio 3D



Recall (old idea)

$$E = \frac{\sigma_x}{\epsilon_x}$$

$$\epsilon_x = \frac{\sigma_x}{E}$$

(New idea)

Poisson's Ratio, ν

$$\nu \equiv - \frac{E \text{ transverse to load direction}}{E \text{ in load direction}}$$

$$\nu = - \frac{\epsilon_y}{\epsilon_x} = - \frac{\epsilon_z}{\epsilon_x}$$

when $\sigma_x \neq 0$: $\epsilon_y = \epsilon_z = -\nu \epsilon_x = -\nu \frac{\sigma_x}{E}$

when $\sigma_y \neq 0$: $\epsilon_x = -\nu \frac{\sigma_y}{E}$; when $\sigma_z \neq 0$: $\epsilon_x = -\nu \frac{\sigma_z}{E}$

3D stress-strain equations

$$\epsilon_x = \frac{\sigma_x}{E} - \nu \frac{\sigma_y}{E} - \nu \frac{\sigma_z}{E}$$

$$\epsilon_y = -\nu \frac{\sigma_x}{E} + \frac{\sigma_y}{E} - \nu \frac{\sigma_z}{E}$$

$$\epsilon_z = -\nu \frac{\sigma_x}{E} - \nu \frac{\sigma_y}{E} + \frac{\sigma_z}{E}$$

Total Strain

$\sigma_x = P_x/A$	$\sigma_x = 0$	$\sigma_x = 0$
$\sigma_y = 0$	$\sigma_y = P_y/A$	$\sigma_y = 0$
$\sigma_z = 0$	$\sigma_z = 0$	$\sigma_z = P_z/A$
$\epsilon_x = \frac{\sigma_x}{E}$	$\epsilon_x = -\nu \frac{\sigma_y}{E}$	$\epsilon_x = -\nu \frac{\sigma_z}{E}$